

1º Caso:  $a \cdot b = c \cdot d$

2º Caso:  $a(a+b) = c(c+d)$

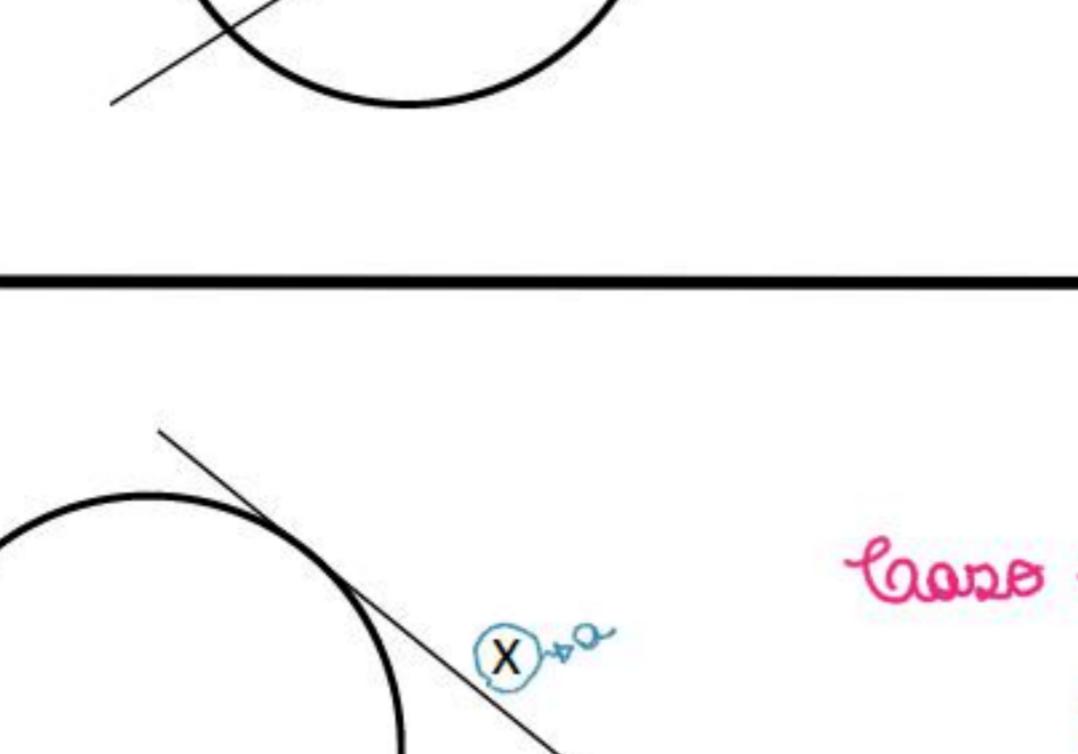
Extremo. Total

$$\frac{a^2}{a} = b(b+c) \rightarrow \text{interno}$$

externo

Em cada caso, determine a incógnita:

1.



2º Caso:

$$a(a+b) = c(c+d)$$

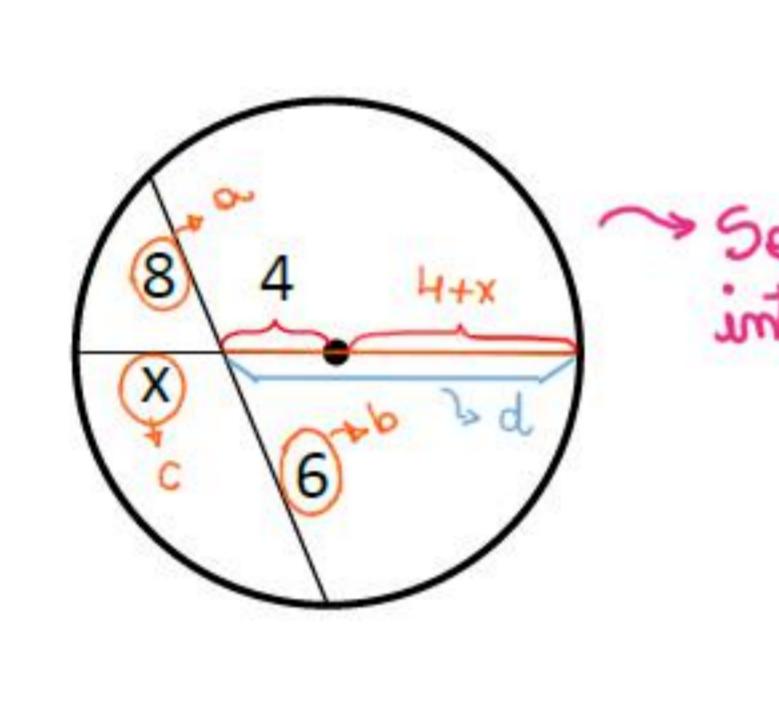
$$4(4+5) = 3(3+x)$$

$$4 \cdot 9 = 9 + 3x$$

$$3x = 27$$

$$\boxed{x = 9}$$

2.



$$\text{Caso} = a^2 = b(b+c)$$

$$x^2 = 2(2+6)$$

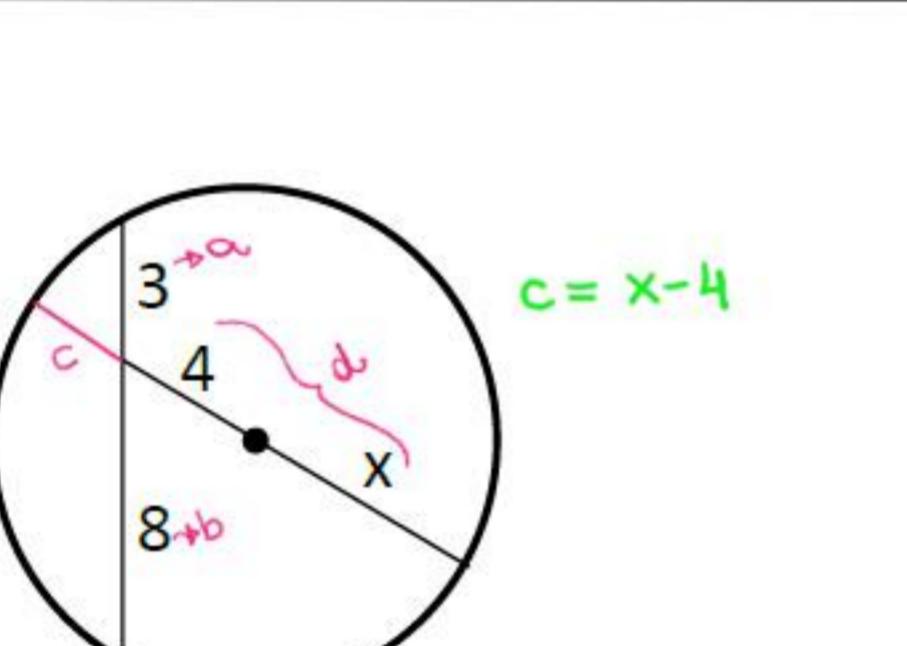
$$x^2 = 2 \cdot 8$$

$$x^2 = 16$$

$$\text{negativo} \rightarrow x = \pm 4$$

$$\boxed{x = 4}$$

3.



2º Caso:

$$a \cdot b = c \cdot d$$

$$8 \cdot 6 = x \cdot (4 + (4+x))$$

$$48 = x \cdot (x+8)$$

$$48 = x^2 + 8x$$

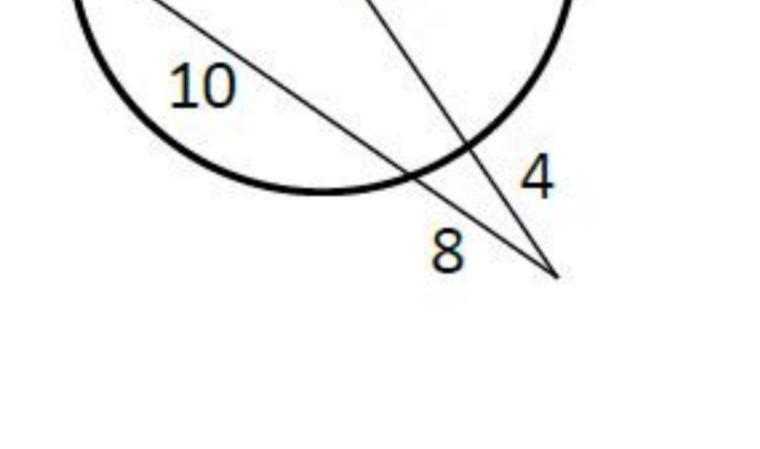
$$x^2 + 8x - 48 = 0$$

$$\frac{4}{4} + \frac{(-12)}{4} = -b/a = -8$$

$$\frac{4}{4} \cdot \frac{(-12)}{4} = +c/a = -48$$

$$\text{Logo, } \boxed{x = 4}$$

4.



$$c = x-4$$

1º Caso:

$$a \cdot b = c \cdot d$$

$$3 \cdot 8 = (4+x) \cdot (x-4)$$

$$24 = -16 - 4x + 4x + x^2$$

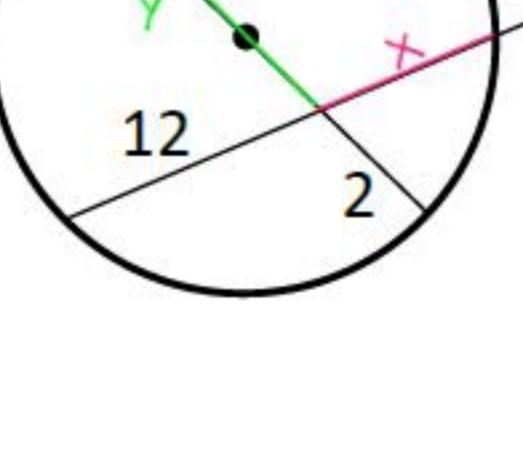
$$x^2 = 16 + 24$$

$$\hookrightarrow x = \sqrt{40} \rightarrow x = \sqrt{4 \cdot 10}$$

$$\boxed{x = 2\sqrt{10}}$$

Determine o raio do círculo em cada caso:

5.



2º Caso:

$$a(a+b) = c(c+d)$$

$$8 \cdot (8+10) = 4 \cdot (4+d)$$

$$144 = 16 + 4d$$

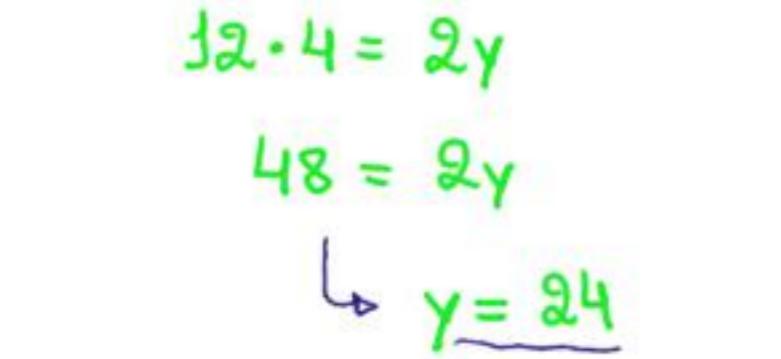
$$\hookrightarrow 4d = 144 - 16$$

$$\hookrightarrow 4d = 128 \rightarrow d = 32$$

Logo,

$$\boxed{r = 36}$$

6.



Temos dois casos:

2º Caso:

$$5 \cdot (5+11) = 4 \cdot (4+(x+12))$$

$$5 \cdot 16 = 4 \cdot (x+16)$$

$$80 = 4x + 64$$

$$4x = 16$$

$$\boxed{x = 4}$$

1º Caso:

$$12 \cdot x = 2 \cdot y$$

$$12 \cdot 4 = 2y$$

$$48 = 2y$$

$$\hookrightarrow y = 24$$

Como queremos o raio, ele será:

$$r = \frac{2+y}{2}$$

$$r = \frac{2+24}{2} \rightarrow \boxed{r = 13}$$