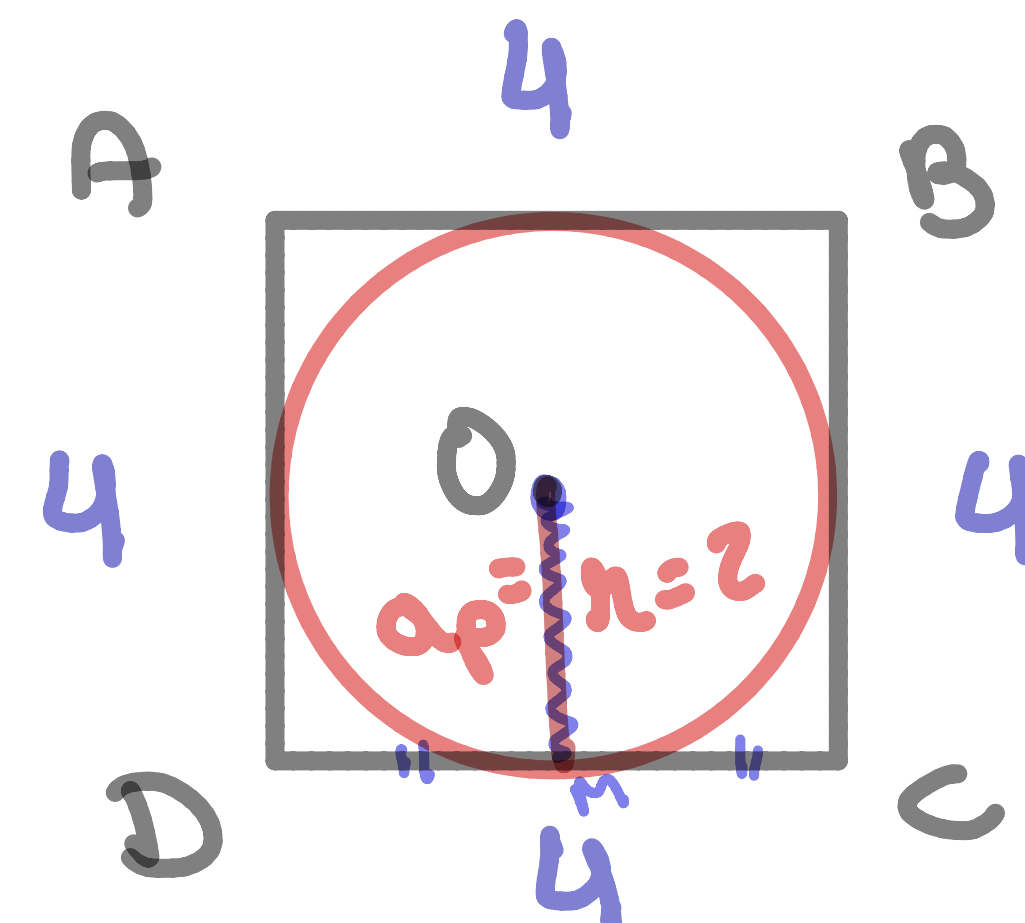


Obs: **Polígonos Regulares** (inscrição e circunscritão)
 (TEM MATH!!!)

Exemplo 11) Determine a medida dos lados dos círculos **INSCRITO** e **CIRCUNSCRITO** a um: **quadrado** de lado 4cm.

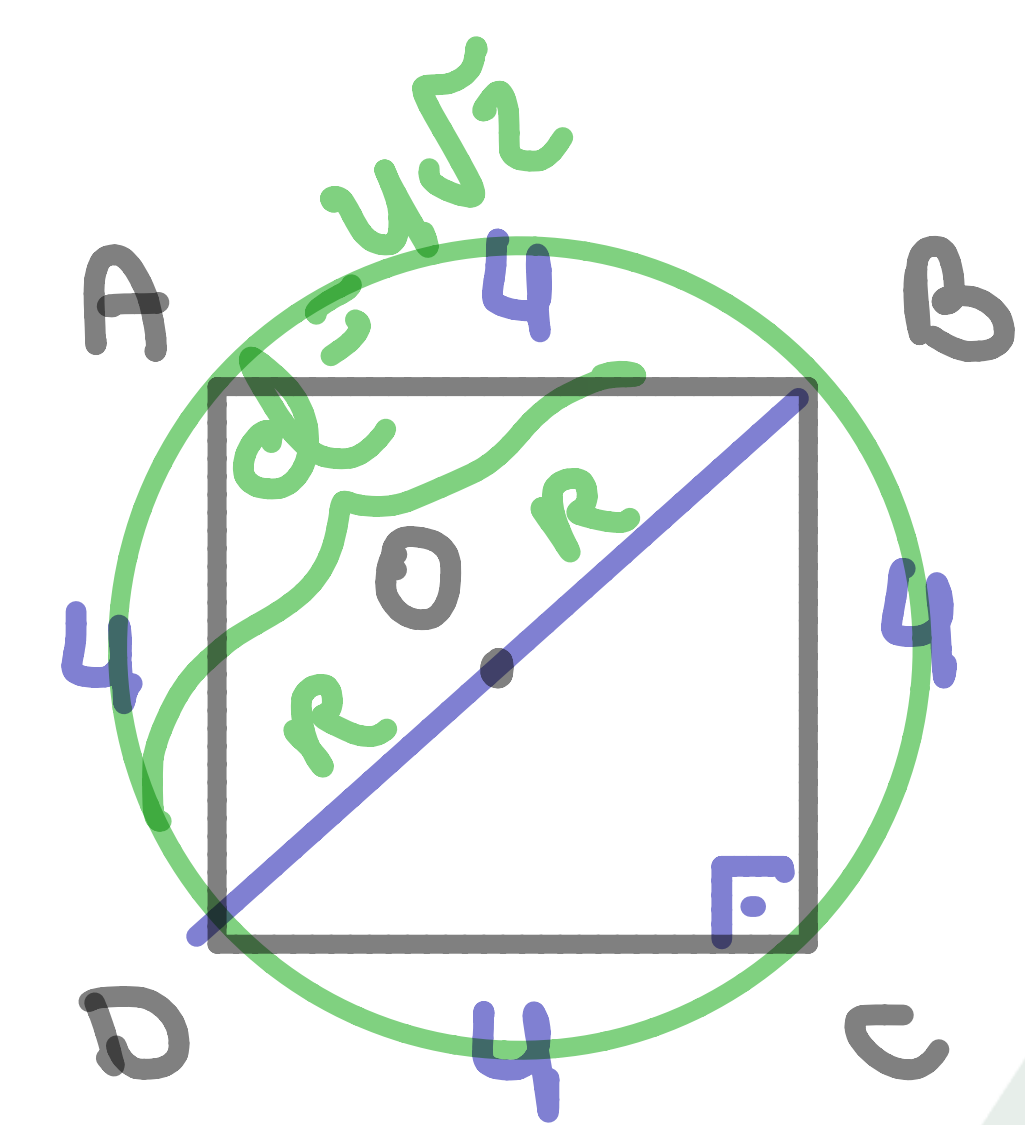
INSCRITO ("dentro") e **CIRCUNSCRITO** ("fora")

a) **quadrado** de lado 4cm.



$n = \frac{l}{2}$

$ap = n = \frac{4}{2} = 2\text{cm}$



$d = l\sqrt{2}$
(diagonal)

$2R = l\sqrt{2}$
 $R = \frac{l\sqrt{2}}{2}$

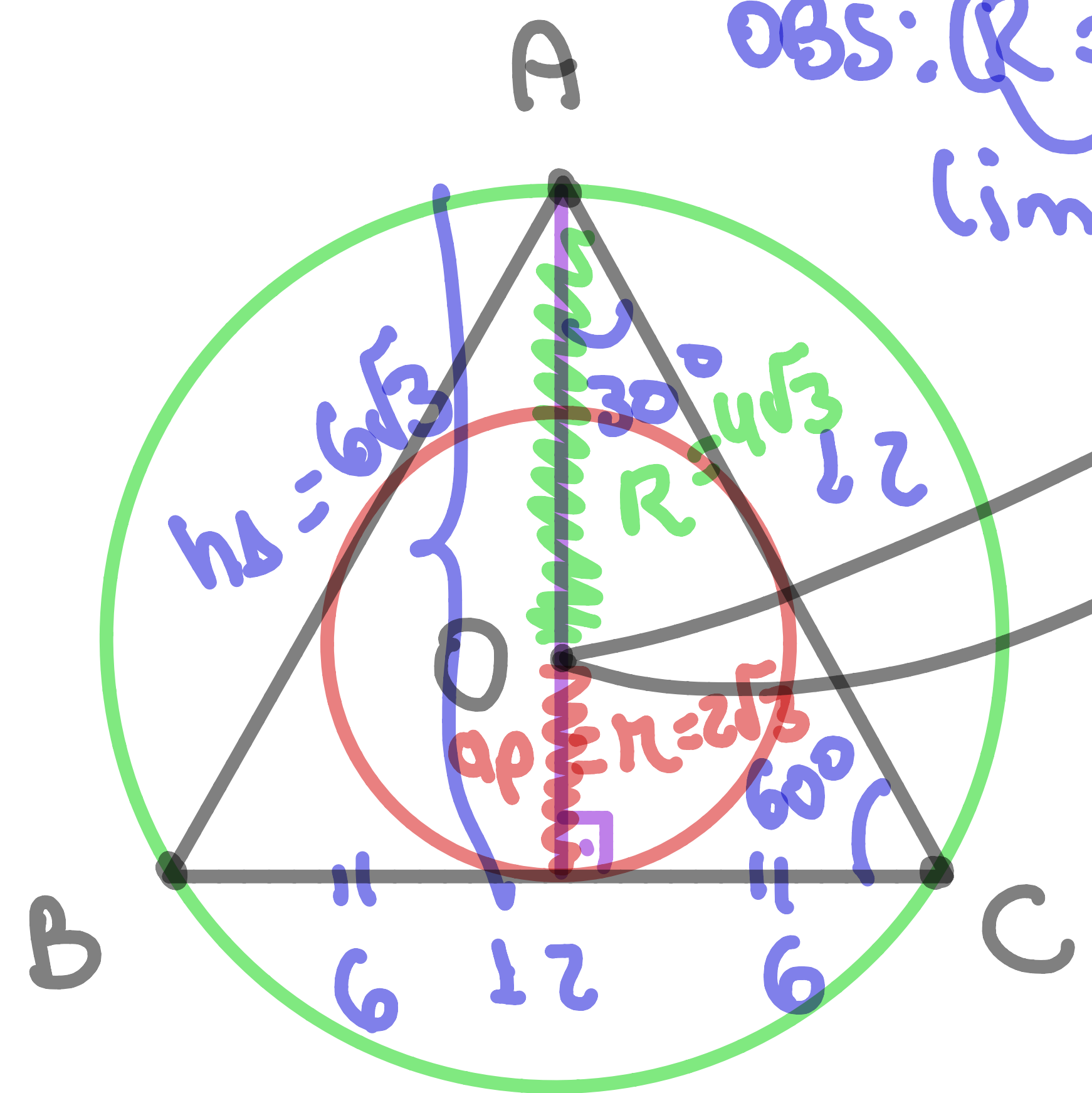
$R = \frac{4\sqrt{2}}{2} = 2\sqrt{2}\text{cm}$

Obs: **APÓTFIMA** \Rightarrow é a distância do centro do polígono regular ao ponto médio de um dos lados.

b) Δ equilátero de altura igual a 12cm.

OBS: (R = 2r)
(importante!)

Como "O" é o
baricentro do
Δ ABC temos:



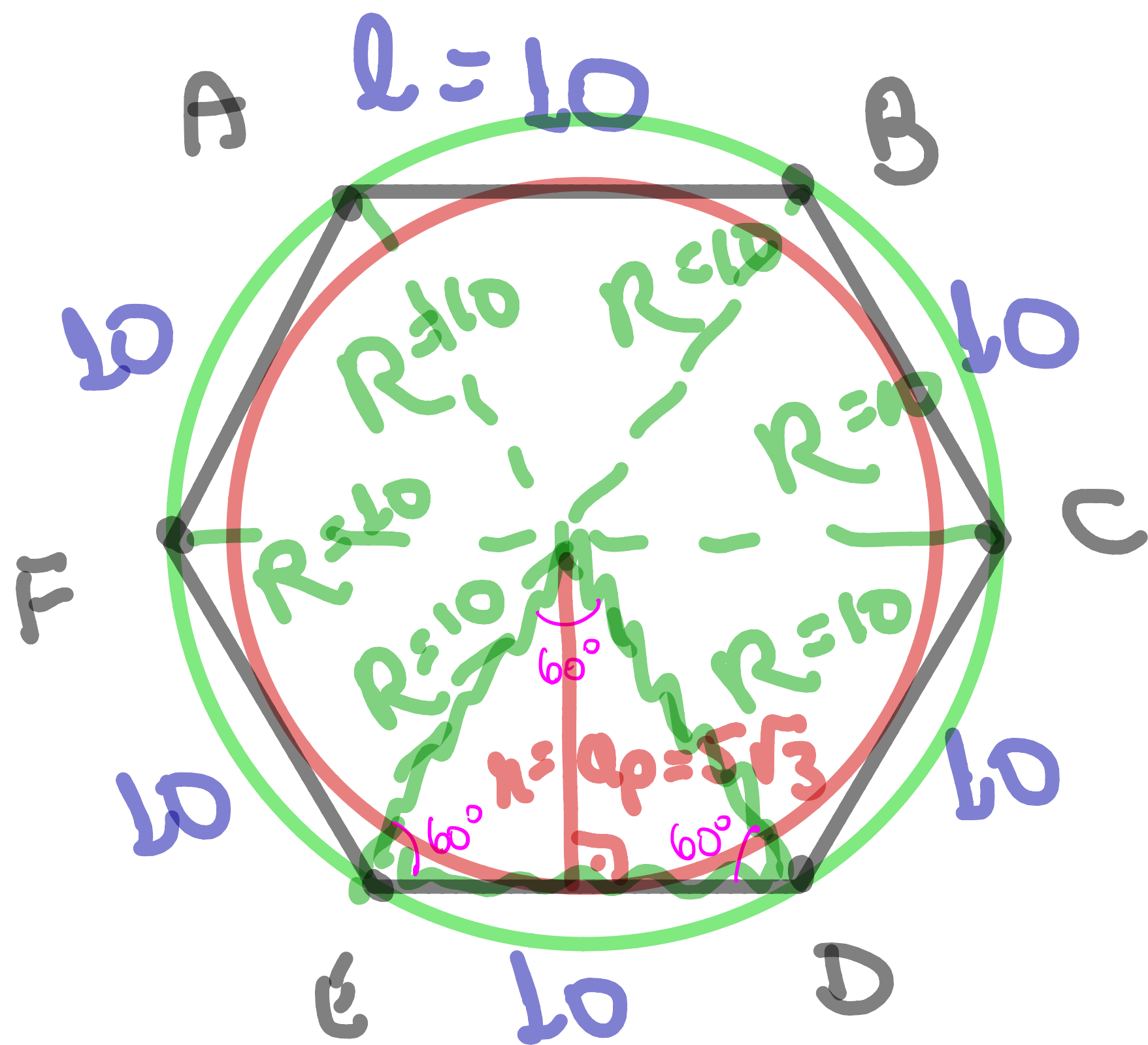
$$a_p = r = \frac{1}{3} h_D = \frac{1}{3} \cdot 6\sqrt{3} = 2\sqrt{3} \text{ cm}$$

$$R = \frac{2}{3} h_D = \frac{2}{3} \cdot 6\sqrt{3} = 4\sqrt{3} \text{ cm}$$

$$\text{ou } h_D = \frac{12\sqrt{3}}{2} = \frac{12\sqrt{3}}{2} = 6\sqrt{3} \text{ cm}$$

c) **Hexágono Regular**
a 60cm.

de perímetro igual



$$R = l_{\text{hex.}} = 10\text{cm}$$

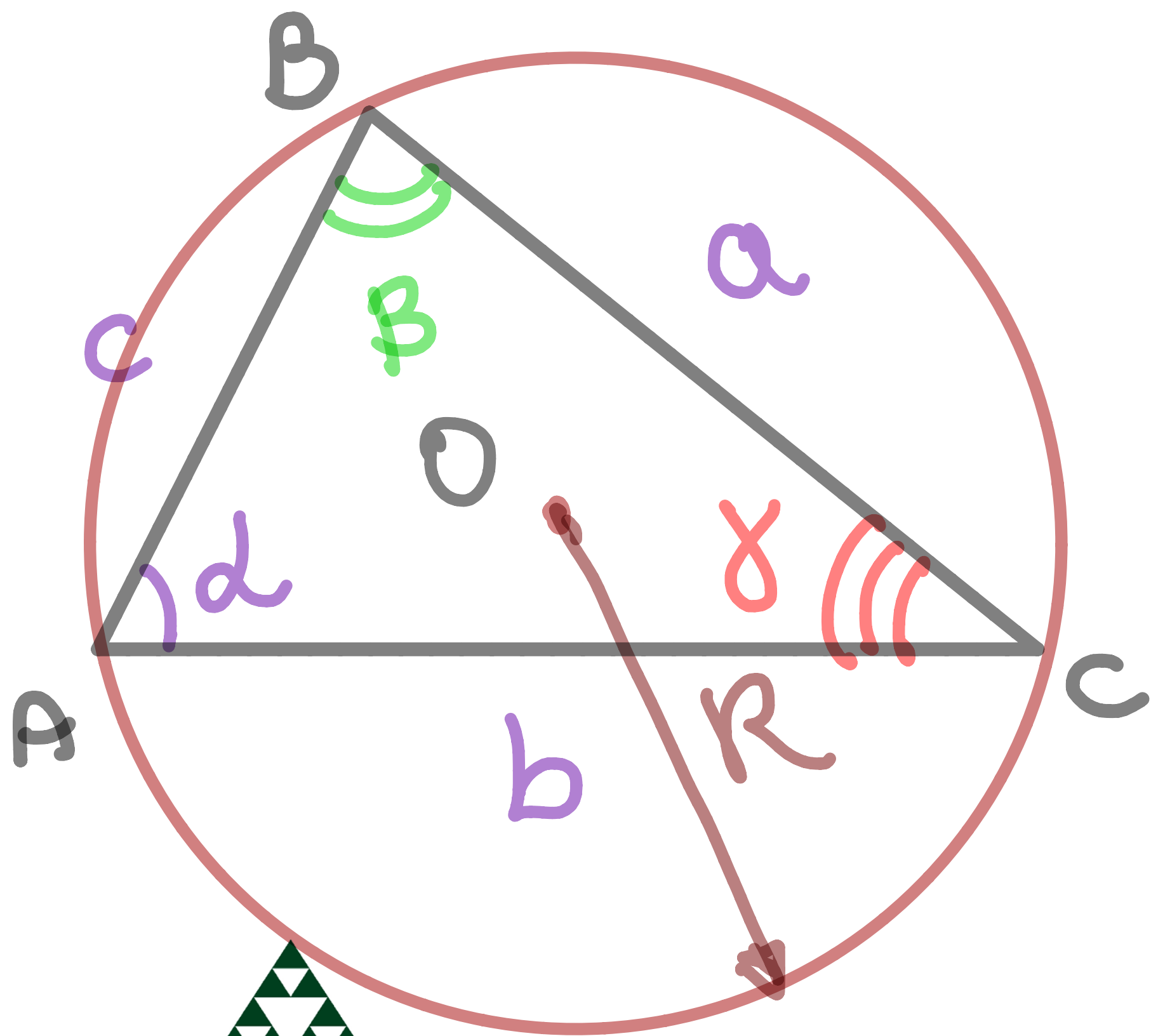
hex.

$$R = h_{\Delta} = \frac{l\sqrt{3}}{2}$$

$$a_p = R = \frac{10\sqrt{3}}{2} = 5\sqrt{3}\text{cm}$$

Relações métricas
no Δ qualquer

(específicas)



Lei dos cossenos

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

$$b^2 = a^2 + c^2 - 2ac \cos \beta$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

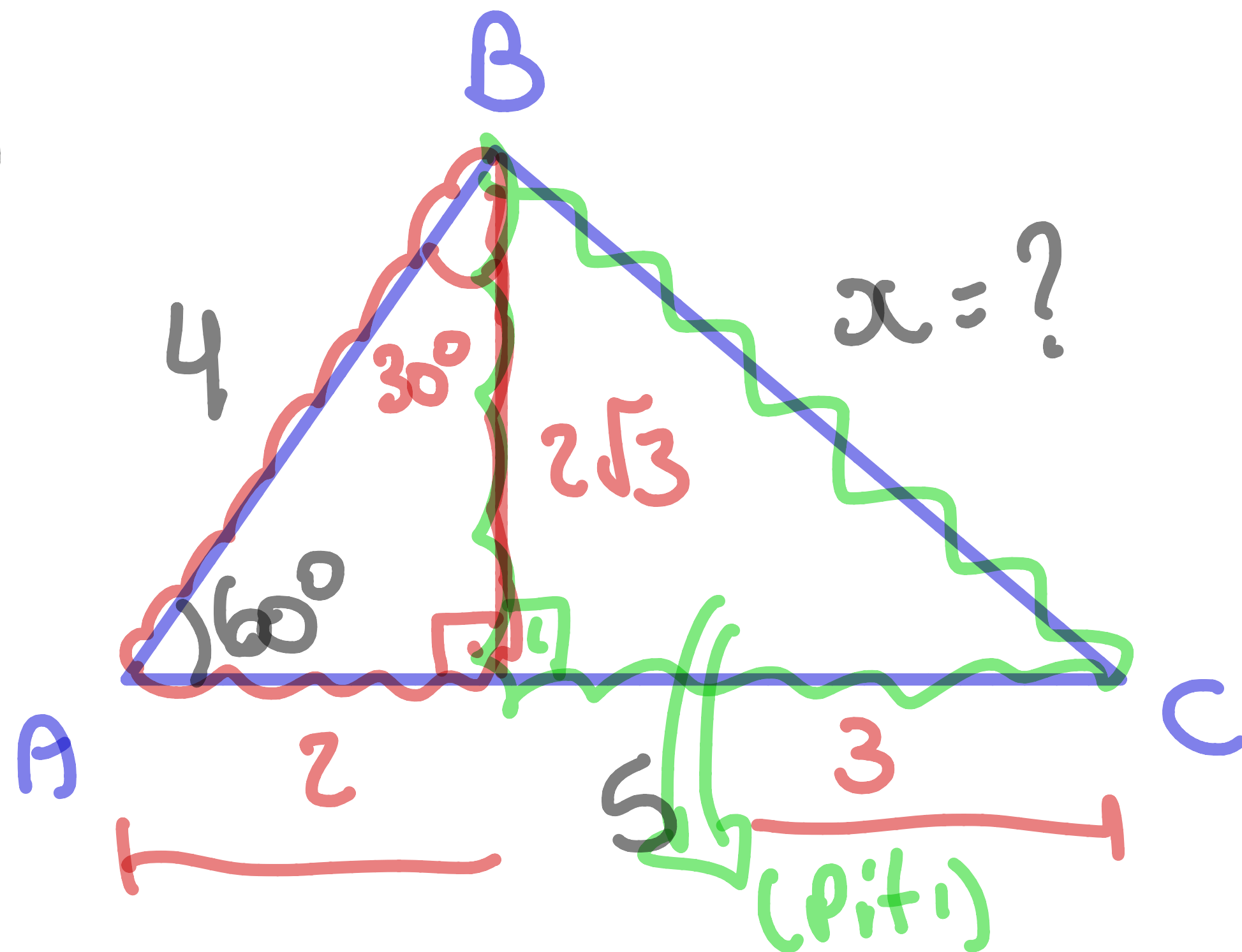
Lei dos senos

$$\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma} = 2R$$

Exemplo 1

Determine o valor de α
nos Δ s abaixo:

a)



$$x^2 = (2\sqrt{3})^2 + 3^2$$

$$x^2 = 12 + 9 \Rightarrow x^2 = 21$$

$$x = \sqrt{21}$$

Lei dos cossenos

$$a^2 = b^2 + c^2 - 2bc \cos A$$

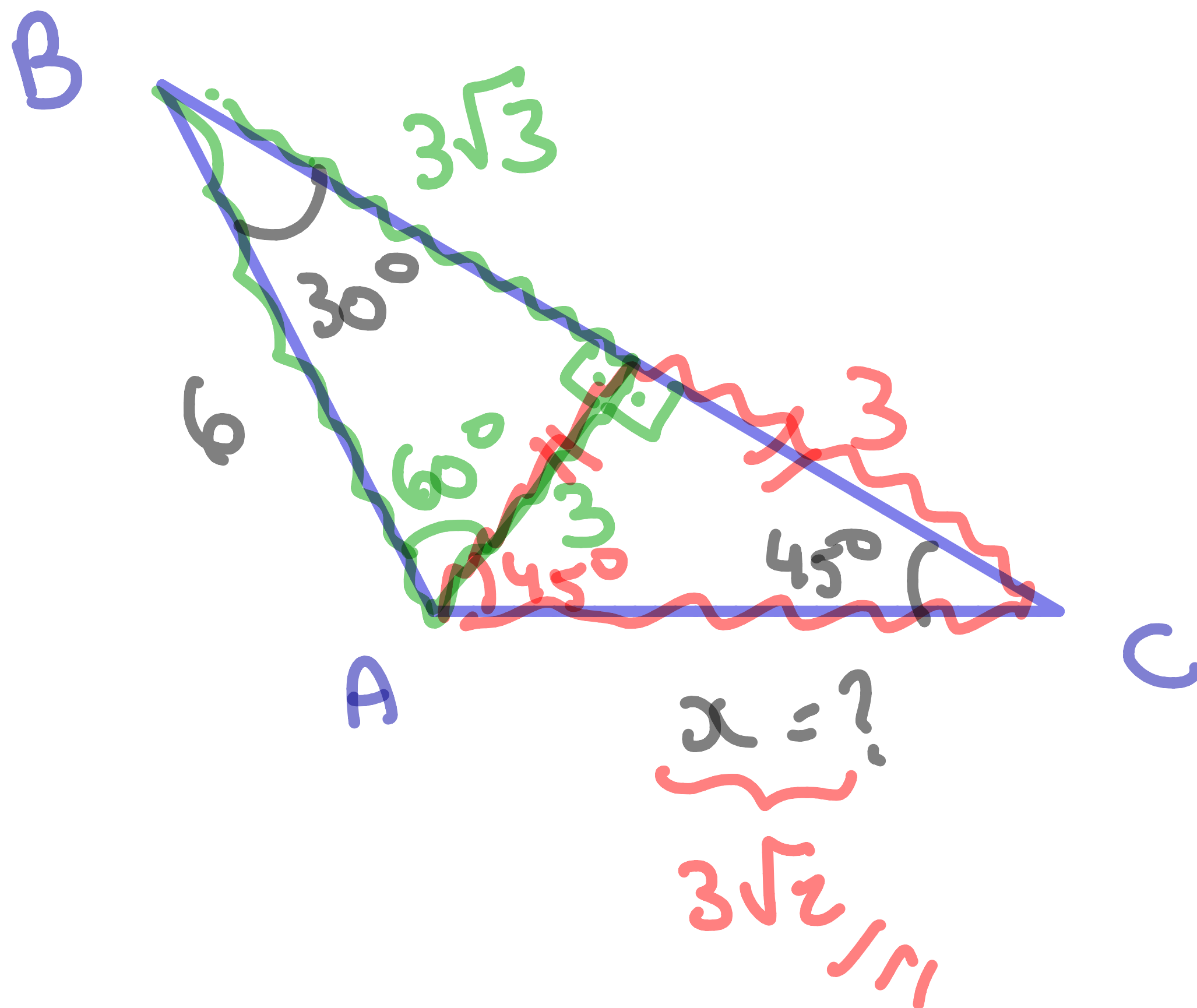
$$x^2 = 4^2 + 5^2 - 2 \cdot 4 \cdot 5 \cdot \cos 60^\circ$$

$$x^2 = 16 + 25 - 40 \cdot \frac{1}{2}$$

$$x^2 = 41 - 20$$

$$x^2 = 21 \Rightarrow x = \sqrt{21}$$

b)



Lei dos Senos

$$\frac{a}{\text{sen } \hat{A}} = \frac{b}{\text{sen } \hat{B}} = \frac{c}{\text{sen } \hat{C}}$$

$$\frac{x}{\text{sen } 30^\circ} = \frac{6}{\text{sen } 45^\circ}$$

$$x \cdot \frac{\sqrt{2}}{2} = 6 \cdot \frac{1}{2}$$

$$x\sqrt{2} = 6$$

$$x = \frac{6}{\frac{\sqrt{2}}{2}} = \frac{6\sqrt{2}}{1} = 3\sqrt{2}$$

c)

$$x \cos 120^\circ = -\cos 60^\circ$$

$$= -\frac{1}{2}$$

(Lei dos cossenos)

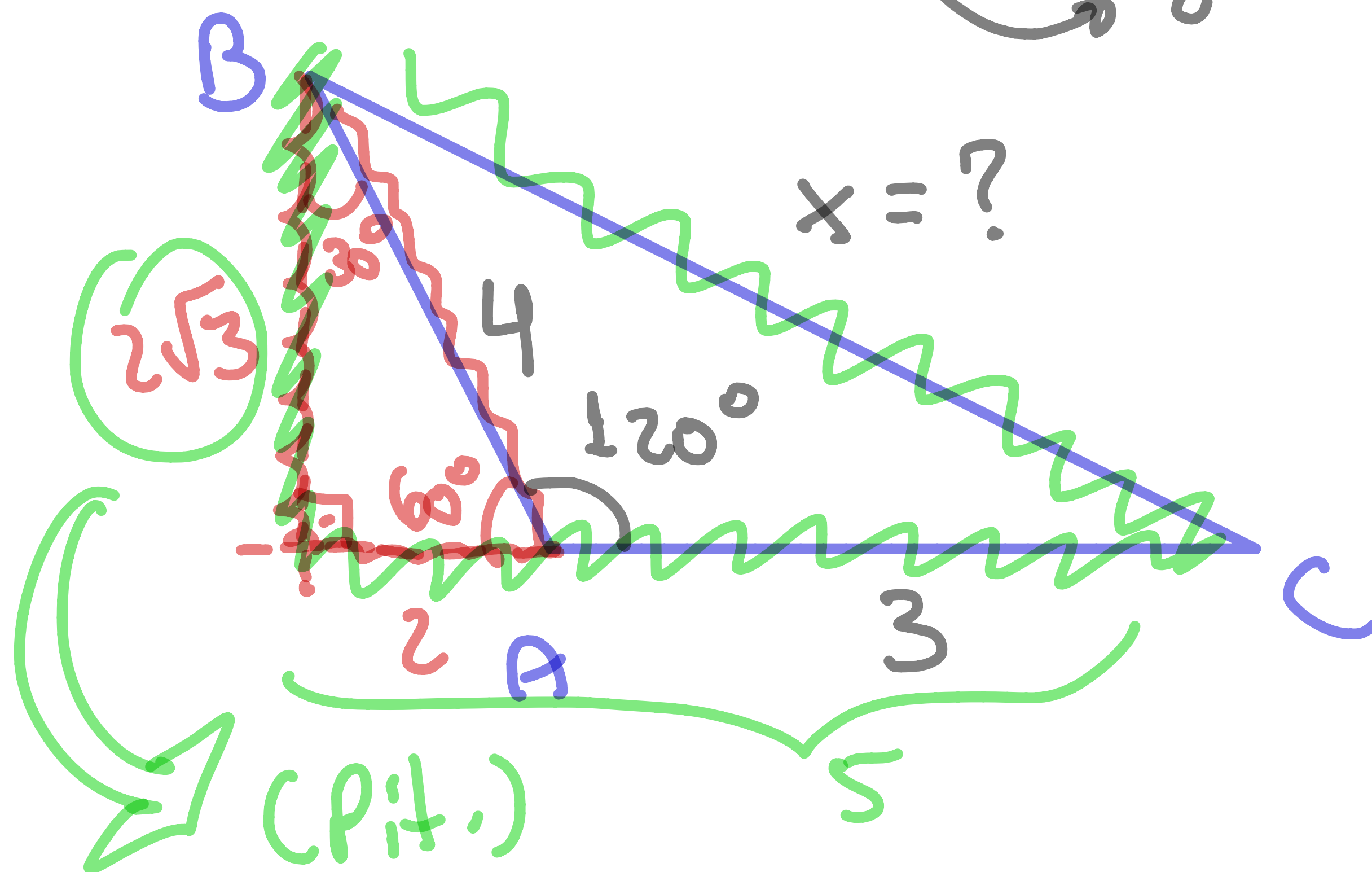
$$x^2 = 4^2 + 3^2 - 2 \cdot 4 \cdot 3 \cos 120^\circ$$

$$x^2 = 16 + 9 - 24 \cdot \left(-\frac{1}{2}\right)$$

$$x^2 = 25 + 12$$

$$x^2 = 37$$

$$x = \sqrt{37}$$



(Pit.)

$$x^2 = (2\sqrt{3})^2 + 5^2$$

$$x^2 = 12 + 25$$

$$x^2 = 37$$

$$x = \sqrt{37}$$